

LFD Rating of Composite Steel Tub Girders in

AASHTOWare BrR

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FDS

- Deliverable AASHTOWare Model of Every Bridge or Unit – 46 total steel units of varying superstructure type and complexity
- To be used in KDOT's **K-TRIPS**:
	- Kansas Truck Routing and Intelligent Permitting System

- o Curved I-Girder Bridges (SFGC, SFCC)
	- Heavy Skew Curved Multi-Girder Systems with Hinges, AASHTOWare 3D FEM
	- Curved Two-Girder Systems with Hinges, AASHTOWare 3D FEM
- o **Straight and Curved Steel Tub Girder Bridges (SBCC)**
	- **Equivalent I-Girder Method in AASHTOWare (presented today)**

- o Tied Arch Bridges (STAT)
	- Floor System in AASHTOWare with external verification to ensure arch ribs, hangers, and ties did not control

- o K-Frame Grasshopper Bridges (SRFC, WRFC)
	- Simplified AASHTOWare Spring Constant Method with external verification to ensure frame legs did not control
	- Once legs shown not to control, simplified AASHTOWare method was used for girders inside AASHTOWare BrR

- o Deck Truss Bridges (SDTS, SDTH, SDTC)
	- AASHTOWare 2D Truss Module
	- Floor System performed in AASHTOWare using:
		- » Floor Line (isolated members)
		- » Floor System

BOX GIRDER LOAD RATING

- Box Girders as Line Girders
	- \circ Goal to get rating factors for shear and moment into one equivalent girder.

$6 - 80$

6B.4-RATING EQUATION

6B.4.1-General

The following general expression should be used in determining the load rating of the structure:

$$
RF = \frac{C - A D}{A_2 L (1 + I)}
$$
 (6B.4.1-1)

where:

 $RF =$ The rating factor for the live load carrying capacity. The rating factor multiplied by the rating vehicle in tons gives the rating of the structure $(see Eq. 6B.4.1-2)$

In the equation above "load effect" is the effect of the applied loads on the member. Typical "load effects" used by engineers are axial force, vertical shear force, bending moment, axial stress, shear stress, and bending stresses. Once the "load effect" to be evaluated is selected by the Engineer, the "capacity" of a member to resist such a load effect may be determined (see Article 6B.5).

$$
RT = (RF)W \tag{6B.4.1-2}
$$

where:

- $RT =$ Bridge member rating (tons)
- $W =$ Weight of nominal truck used in determining the live load effect, L (tons)

The rating of a bridge is controlled by the member with the lowest rating in tons.

BOX GIRDER VS. EQUIVALENT I-GIRDER

- **Box Girder (Fully Composite)**
	- o Web Shear
	- o Web-Bend Buckling
	- o Flange Yield (Top and Bottom Flange)
	- o Local Flange Buckling (Bottom Flange)
	- o No lateral torsional buckling
		- Boxes are 100 to 1000 times torsionally stiff than I-Girders.

- \circ Web Shear
- o Web-Bend Buckling
- o Flange Yield (Top and Bottom Flange)
- o Local Flange Buckling (Bottom Flange)
- \circ Lateral Torsional Buckling (Do not want in equivalent model)
- "Dummy" bracing added at every 5 ft to simulate box girder **VS.** torsional rigidity and ensure lateral torsional buckling in the equivalent I-Girder does not control

ACTUAL BOX GIRDER ½ I-GIRDER EQUIVALENT

- **•** Set $S_{EQ} = \frac{1}{2} S_{BOX}$
- **•** Set $DF_{LLEO} = \frac{1}{2} DF_{LLBOX}$
- **•** Set $F_{\text{crEO}} = F_{\text{crBOX}}$ for bottom flange local buckling
- **•** Set Effwidth_{EQ} = $\frac{1}{2}$ Effwidth_{BOX}
- $f_{EO} = f_{BOX}$ (f = Mc/I = M/S)

BOX/TUB GIRDER OBJECTIVES

- Captured:
	- \circ Load Rating for Major Axis Bending Positive and Negative Flexure, Top and Bottom Flanges
	- o Load Rating for Major Axis Shear Webs
- Not Captured:
	- o St. Venant's Torsional Stresses
	- **Cross-Sectional Distortion Stresses**
	- o System Effects (Line Girder Only)
	- o Skew Effects (Bridges had minor skew or were square)
	- o Curvature Effects (Bridges had minor curvature >5000' radius or were straight)

3)

 \blacksquare AASHTO Std. Spec. 17th Ed. 2002

10.39.3.2 Secondary Bending Stresses

 $10.39.3.2.1$ Web plates may be plumb (90 $^{\circ}$ to bottom of flange) or inclined. If the inclination of the web plates to a plane normal to the bottom flange is no greater than 1 to 4, and the width of the bottom flange is no greater than 20% of the span, then the transverse bending stresses resulting from distortion of the span, and the transverse bending stresses resulting from distortion of the girder cross section and from vibrations of the bottom plate need not be considered. For structures in this category transverse bending stresses due to supplementary loadings, such as utilities, shall not exceed 5,000 psi.

10.39.3.2.2 For structures exceeding these limits, a detailed evaluation of the transverse bending stresses due to all causes shall be made. These stresses shall be limited to a maximum stress or range of stress of 20,000 psi.

▪ AASHTO LRFD 2014

6.11.1.1-Stress Determinations

Box flanges in multiple and single box sections shall be considered fully effective in resisting flexure if the width of the flange does not exceed one-fifth of the effective span. For simple spans, the effective span shall be taken as the span length. For continuous spans, the effective span shall be taken equal to the distance between points of permanent load contraflexure, or between a simple support and a point of permanent load contraflexure, as applicable. If the flange width exceeds one-fifth of the effective span, only a width equal to onefifth of the effective span shall be considered effective in resisting flexure.

For multiple box sections in straight bridges satisfying the requirements of Article 6.11.2.3, the live-load flexural moment in each box may be determined in accordance with the applicable provisions of Article 4.6.2.2.2b. Shear due to St. Venant torsion and transverse bending and longitudinal warping stresses due to cross-section distortion may also be neglected for sections within these bridges that have fully effective box flanges. The section of an exterior member assumed to resist horizontal factored wind loading within these bridges may be taken as the bottom box flange acting as a web and 12 times the thickness of the web acting as flanges.

EQUIVALENT STRESSES: BOX GIRDER VS. EQUIVALENT I-GIRDER

- \cdot $\frac{1}{2}$ Girder Steel = $\frac{1}{2}$ Steel Dead Load
- $\frac{1}{2}$ Effective Deck Width = $\frac{1}{2}$ Effective Deck Section for n and 3n
- ½ Tributary Deck Width = ½ Concrete Dead Load
- $\frac{1}{2}$ Live Load Distribution Factor = $\frac{1}{2}$ Live Load (Moment, Shear)

EQUIVALENT SHEAR FORCE: BOX GIRDER VS. EQUIVALENT I-GIRDER

- With C factor included in calculation, \sim 2% error or less in most cases with ${\sf d}_0$ normalized over the difference in D of the web
	- \blacksquare AASHTO Std. Spec. 17th Ed. 2002

10.48.8 Shear

10.48.8.1 The shear capacity of webs of rolled or fabricated flexural members shall be computed as follows:

For unstiffened webs, the shear capacity shall be limited to the plastic or buckling shear force as follows:

$$
V_u = CV_p \tag{10-113}
$$

For stiffened web panels complying with the provisions of Article 10.48.8.3, the shear capacity shall be determined by including post-buckling resistance due to tension-field action as follows:

$$
V_{u} = V_{p} \left[C + \frac{0.87(1 - C)}{\sqrt{1 + (d_{o}/D)^{2}}} \right]
$$
 (10-114)

 V_p is equal to the plastic shear force and is determined as follows:

$$
V_p = 0.58F_y Dt_w
$$
 (10-115)

The constant C is equal to the buckling shear stress divided by the shear yield stress, and is determined as follows:

LIVE LOAD DISTRIBUTION

\blacktriangleright AASHTO Std. Spec. 17th Ed. 2002

10.39.2 Lateral Distribution of Loads for Bending **Moment**

10.39.2.1 The live load bending moment for each box girder shall be determined by applying to the girder, the fraction W_L of a wheel load (both front and rear), determined by the following equation:

$$
W_{L} = 0.1 + 1.7R + \frac{0.85}{N_{w}}
$$
 (10-70)

where

$$
R = \frac{N_w}{Number of Box Girders}
$$
 (10-71)

 $N_w = W_c/12$ reduced to the nearest whole number; W_c = roadway width between curbs in feet, or barriers if curbs are not used. R shall not be less than 0.5 or greater than 1.5.

• Compute DF of actual box girder

LIVE LOAD DISTRIBUTION

1.040

1.040

1.040

1.040

Supports

0.795

 1.310

1.040

1.040

• DF Equivalent I-Girder = $\frac{1}{2}$ **DF Actual Box Girder**

1 Lane

Multi-Lane

SETTING SECTION GEOMETRY – ACTUAL BOX

- For every longitudinal section
	- o Steel Only Section DC1 Load
	- \circ n Section Transient Short-Term Live Load
	- \circ 3n Section Long-Term Dead Load (DC2, DW)

SETTING SECTION GEOMETRY – ACTUAL BOX (CONT.)

Box Girder: Calculate Local Buckling Capacity of Bottom Flange of Actual Box girder at All Sections (AASHTO Std. Spec. 10.51.5)

10.51.5.4 If longitudinal stiffeners are used, they shall be equally spaced across the flange width and shall be proportioned so that the moment of inertia of each stiffener about an axis parallel to the flange and at the base of the stiffener is at least equal to

$$
I_s = \phi t^3 w \tag{10-138}
$$

where

 $\phi = 0.07k^3n^4$ when n equals 2, 3, 4, or 5;

 $\phi = 0.125k^3$ when $n = 1$:

- $w =$ width of flange between longitudinal stiffeners or distance from a web to the nearest longitudinal stiffener:
- $n = number of longitudinal stiffness$:
- $k =$ buckling coefficient which shall not exceed 4.

$10.51.5.4.1$

For a longitudinally stiffened flange designed for the yield stress F_y, the ratio w/t shall not exceed the value given by the formula

$$
\frac{w}{t} = \frac{3,070\sqrt{k}}{\sqrt{F_y}}
$$
 (10-139)

10.51.5.4.2 For greater values of w/t

$$
\frac{3,070\sqrt{k}}{\sqrt{F_y}} < \frac{w}{t} \le \frac{6,650\sqrt{k}}{\sqrt{F_y}}
$$
 (10-140)

the buckling stress of the flange, including stiffeners, is given by Article 10.51.5.2 in which c shall be taken as

$$
c = \frac{6,650\sqrt{k} - \frac{w}{t}\sqrt{F_y}}{3,580\sqrt{k}}
$$
 (10-141)

10.51.5.4.3 For values of

$$
\frac{w}{t} > \frac{6,650\sqrt{k}}{\sqrt{F_{\gamma}}}
$$
 (10-142)

the buckling stress of the flange, including stiffeners, is given by the formula

> $F_{cr} = 26.2k(t/w)^{2} \times 10^{6}$ $(10-143)$

• For every longitudinal section transition

o Calculate Actual Bottom Flange Buckling Capacity

DOUBLE ITERATION OF BOTTOM FLANGE

2 Braced Noncompact Sections

sections of rolled or fabricated flexural members eeting the requirements of Article 10.48.1.1 but ig the requirements of Article 10.48.2.1 below, the um strength shall be computed as the lesser of

$$
M_a = F_y S_{xt} \tag{10-98}
$$

 $M_u = F_c S_{sc} R_h$ $(10-99)$

to the requirement of Article 10.48.2.1(c) where

- All critical buckling stresses Box vs. Equivalent I-Girder within 1% or less
- \blacktriangleright All bottom flange areas $\frac{1}{2}$ Box vs. Equivalent I-Girder within 1% or less
	- \circ Contributes to section property comparison of section moduli (S, in^{\land 3)}

SECTION PROPERTY COMPARISON: ACTUAL BOX VS. EQUIVALENT I-GIRDER

- \blacksquare All Sections Section Moduli Within \sim 3% or less
- \cdot S=I/c

BOX GIRDERS WITH OR WITHOUT LONGITUDINAL STIFFENERS

- b/t ratio of bottom flange of equivalent I-Girder can be iterated to match the local buckling capacity of the bottom flange of an actual box section with or without longitudinal stiffeners
- On KDOT Load Rating Project we had both scenarios

SECTION GEOMETRY IN AASHTOWARE BRR

TRANSVERSE STIFFENERS

- Transverse Stiffener Spacing and Geometry
	- \circ Same as actual box girder web
- **Exercise 1** Fictional diaphragms every 5 to 6 ft simulates box girder torsional rigidity, ensures lateral torsional buckling doesn't control rating

Diaphragms Lateral Support Ranges | Lateral Support Locations

Transverse Stiffener Ranges Longitudinal Stiffener Ranges

KDOT LOAD RATING VEHICLES

 $\left| \Xi \right|$.

Span 2 – 17.50 ft Longitudinal Stiffener Termination Location

▪ Even though Iyc/Iy falls outside of 0.1 and 0.9 limits, AASHTOWare still computes Mr

SUMMARY:

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(a) Compression flange proportionality
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Ivc
0.1 \leq - - - - - \leq 0.9Iy
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Mu = Mr*Rb*R(10-103a)
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where, $Mr = partially$ braced resistance moment, $10.48.4.1$ Rb = web slenderness ratio, 10.48.4.1 $R =$ hybrid reduction factor, 10.53.1.2

RESULTS:

Top flange $Iyt/Iy = 0.039$ (Fail) Bot flange $Iyb/Iy = 0.961$ (Fail)

Span 2 - 43.50 ft.

RESULTS:

Note - Bottom flange b/t is too large. Minimum capacity between 10.48.2 and 10.48.4.1 will be used.

10.48.4 Partially Braced Members

Members not meeting the lateral bracing requirement of Article 10.48.2.1(c) shall be braced at discrete locations spaced at a distance, L_b , such that the maximum strength of the section under consideration satisfies the requirements of Article 10.48.4.1. Bracing shall be provided such that lateral deflection of the compression flange is restrained and the entire section is restrained against twisting.

10.48.4.1 If the lateral bracing requirement of Article 10.48.2.1(c) is not satisfied and the ratio of the moment of inertia of the compression flange to the moment of inertia of the member about the vertical axis of the web. I_{yz}/I_{y} , is within the limits of 0.1 $\leq I_{yz}/I_{y} \leq 0.9$, the maximum strength for the limit state of lateral-torsional buckling shall be computed as

10.48.2 Braced Noncompact Sections

For sections of rolled or fabricated flexural members not meeting the requirements of Article 10.48.1.1 but meeting the requirements of Article 10.48.2.1 below, the maximum strength shall be computed as the lesser of

$$
M_u = F_y S_{xt} \tag{10-98}
$$

OI

$$
M_u = F_{cr} S_{xc} R_b \tag{10-99}
$$

subject to the requirement of Article 10.48.2.1(c) where

 $F_{cr} = \left(4,400 \frac{t}{b}\right)^2 \le F_y$

 $\mathcal{L}_{\mathcal{A}}$

in Li

10.50.2.2 Noncompact Sections

When the steel section does not satisfy the compactnes requirements of Article 10.50.2.1 but does satisfy all the requirements of Article 10.48.2.1, the sum of the bending stresses due to the appropriate loadings acting on the re-

- The girder does not satisfy noncompact criteria for compressive strength so AASHTOWare takes the minimum of the partially braced compressive capacity or the local flange buckling capacity.
- Since the partially braced capacity is Fy due to the fictional bracing input at every 5', local flange buckling controls
- Therefore, for the bottom flange, AASHTOWare checks capacity to Fy and Fcr only, mimicking the behavior of the actual box girder
- F Fcr = 4.86 ksi
- S, negative moment = 691.73 in^{3}
- \blacksquare Mu=Fcr x S
- Mu=4.86 ksi x 691.73 in^3 x 1/12 in = 280 k-ft (verified)

FINAL BOX GIRDER RATING SUMMARY

• N.B. I-635 over F.B. I-35

▪ Results:

- o typically areas of high moment or areas with abrupt changes in capacities i.e. flange transitions or longitudinal stiffener termination locations controlled the rating
- o Shear controlled rating for areas of high shear, heavy axles on various trucks, panel length changes due to changes in transverse stiffener spacing

• Modeling of K-Frame Grasshopper Bridges using simplified spring method with external verification

• I-435 over I-70

سمعيد

• Modeling of K-Frame Grasshopper Bridges using simplified spring method with external verification

Min_Br_No_0105-B0213_214.std - Whole Structure

■ Modeling of K-Frame Grasshopper Bridges using simplified spring method with external verification

(Deflections not to Scale)

▪ Modeling of K-Frame Grasshopper Bridges using simplified spring method with external verification

▪ Modeling of K-Frame Grasshopper Bridges using simplified spring method with external verification

Leg ₁					
Flexure					
Top Flange			Bottom Flange		
Min RF	xlocation (along leg)	truck location	Min RF	xlocation	truck location
3.36	0.00	164.00	4.24	0.00	164.00
Shear					
Min RF	xlocation (along leg)	truck location			
3.65	20.71	164.00			
Axial (weak)					
Min RF	xlocation (along leg)	truck location			
10.65	21.38	94.00			
Axial (strong)					
Min RF	xlocation (along leg)	truck location			
10.46	21.38	94.00			
Combined Axial (Strong Axis) and Flexure					
Min RF	xlocation (along leg)	truck location			
3.34	0.00	160.00			
Leg ₂					
Flexure					
Top Flange			Bottom Flange		
Min RF	xlocation (along leg)	truck location	Min RF	xlocation	truck location
3.82	0.00	112.00	4.96	0.00	234.00
Shear					
Min RF	xlocation (along leg)	truck location			
4.19	20.97	112.00			
Axial (weak)					
Min RF	xlocation (along leg)	truck location			
10.67	21.64	182.00			
Axial (strong)					
Min RF	xlocation (along leg)	truck location			
10.48	21.64	182.00			
Combined Axial (Strong Axis) and Flexure					
Min RF	xlocation (along leg)	truck location			
3.74	0.00	116.00			

▪ Modeling of K-Frame Grasshopper Bridges using simplified spring method with external verification

• AASHTOWare BrR • STAAD FEM/Excel Post-Processing

- Modeling of Hinges (Shelf Plate) in 3D FEM I-Girder Models
- Moment to "zero" at hinge, shear carried across hinge, hinges rated for local moment externally using shear force generated from AASHTOWare model

▪ Modeling of Hinges (Shelf Plate) in 3D FEM I-Girder Models

▪ Moment Diagram: Example Bridge with Hinges

■ Reverse Curvature Bending in longitudinal members

▪ Reverse Curvature Bending in longitudinal members

- Reverse Curvature Bending in longitudinal members
	- \circ C_b factor modification
	- \blacksquare 2014 AASHTO LRFD 7th Edition, 6.10.8.2.3 (LTB) \blacksquare 2014 AASHTO LRFD 7th Edition, C6.10.8.2.3

$$
F_{nc} = C_b \left[1 - \left(1 - \frac{F_{yr}}{R_h F_{yc}} \right) \left(\frac{L_b - L_p}{L_r - L_p} \right) \right] R_b R_h F_{yc} \le R_b R_h F_{yc}
$$
\n(6.10.8.2.3-2)

If $L_k > L_r$, then: \bullet

$$
F_{nc} = F_{cr} \le R_b R_h F_{yc}
$$
 (6.10.8.2.3-3)

- For unbraced cantilevers and for members where $f_{mid}/f_2 > 1$ or $f_2 = 0$ $C_{k} = 1.0$ $(6.10.8.2.3-6)$
- For all other cases:

$$
C_b = 1.75 - 1.05 \left(\frac{f_1}{f_2}\right) + 0.3 \left(\frac{f_1}{f_2}\right)^2 \le 2.3 \quad (6.10.8.2.3-7)
$$

For unbraced lengths where the member consists of monosymmetric noncomposite I-sections and is subject to reverse curvature bending, the lateral torsional buckling resistance must be checked in general for both flanges, unless the top flange is considered to be continuously braced. Since the flanges are of different sizes in these types of sections, the lateral torsional buckling resistance may be governed by compression in the smaller flange, even though this compressive stress may be smaller than the maximum compression in the larger flange. The specified approach generally produces accurate to conservative values of C_b for these cases. For highly

 $(C-F[-])$

\blacksquare AISC Steel Manual, 14th Edition

Since 1961, the following equation has been used in AISC Specifications to advertise the lateral-torsional buckling equations for variations in the moment diagram with the unbraced length.

$$
C_b = 1.75 + 1.05 \left(\frac{M_1}{M_2}\right) + 0.3 \left(\frac{M_1}{M_2}\right)^2
$$

where

 M_1 = smaller moment at end of unbraced length, kip-in. (N-mm)

 M_2 = larger moment at end of unbraced length, kip-in. (N-mm)

 (M_1/M_2) is positive when moments cause reverse curvature and negative for single curvature

This equation is only applicable to moment diagrams that consist of straight lines between braced points—a condition that is rare in beam design. The equation provides a lower bound to the solutions developed in Salvadori (1956). Equation C-FIcan be easily misinterpreted and misapplied to moment diagrams that are not linear within the unbraced segment. Kirby and Nethercot (1979) present an equation that applies to various shapes of moment diagrams within the unbraced segment. Their original equation has been slightly adjusted to give Equation C-F1-2 (Equation F1-1) in the body of the Specification):

> $C_b = \frac{12.5M_{max}}{2.5M_{max} + 3M_A + 4M_B + 3M_C}$ $(C-F1-2)$

This equation gives a more accurate solution for a fixed-end beam, and gives approximately the same answers as Equation C-F1-1 for moment diagrams with straight lines between points of bracing. C_b computed by Equation C-F1-2 for moment diagrams with other shapes shows good comparison with the more precise but also more complex equations (Ziemian, 2010). The absolute values of the three quarter-point moments and the maximum moment regardless of its location are used in Equation C-F1-2. The maximum moment in the unbraced segment is always used for comparison with the nominal moment, M_n . The length between braces, not the distance to inflection points is used. It is still satisfactory to use C_b from Equation C-F1-1 for straight-line moment diagrams within the unbraced length.

- Reverse Curvature Bending in longitudinal members
	- \circ C_b factor modification

▪ 1961 AASHO

Compression in extreme fibers of rolled shapes, girders and built sections, subject to bending, gross section.

ntilever beams or girders may be proportioned for negative moment at interior supports for an allowable unit stress 20 per cent higher than permitted
by shows formula but in no one are discussed unit stress 20 per cent higher than permitted by above formula but in no case excreding allowable unit stress 20 per cent higher than permitted
ported its full length. If cover plates are used, the allowable unit of the ported its full length and the plates are used, shall be as determined by the formula.

- Reverse Curvature Bending in longitudinal members
	- o Braces at DL inflection points
	- \circ Hand calculations to verify C_b with AISC Equations after braces are added

QUESTIONS?

